SYDNEY TECHNICAL HIGH SCHOOL



TRIAL HIGHER SCHOOL CERTIFICATE

2008

MATHEMATICS

Time Allowed: 3 hours plus 5 minutes reading time

Instructions:

- Write your name and class at the top of this page, and at the top of each answer sheet
- At the end of the examination this examination paper must be attached to the front of your answers
- All questions are of equal value and may be attempted
- All necessary working must be shown. Marks may not be awarded for careless or badly arranged work.
- Marks indicated are a guide only and may be varied if necessary.

(for Markers Use Only)

Q1	Q2	Q3	Q4	Q5	Q6	Q7	Q8	Q9	Q10	Total

Question 1 (12 marks)

a) Find $e^{-0.6}$ correct to 3 decimal places.

b) Expand and simplify $(\sqrt{2}-3)^2$

c) Given $\frac{1}{P} = \frac{1}{Q} + \frac{1}{R}$ make Q the subject of the formula.

d) (i) Find $\int_{1}^{2} \frac{dx}{x}$

(ii) Evaluate $\int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \cos\left(\frac{x}{2}\right) dx$. Leave your answer as an exact value.

e) Solve the inequality $|2x - 3| \le 7$

f) Solve the following equations simultaneously

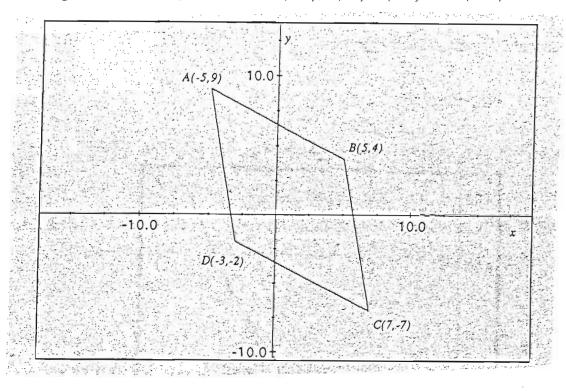
$$2x + y = 4$$

5x + 2y = 9

Question 2 (Use a separate sheet of paper) (12 marks)

a) A rhombus is a parallelogram with four sides of equal length.

The figure shown below, with vertices A(-5,9), B(5,4), C(7,-7) and D(-3,-2) is a rhombus.

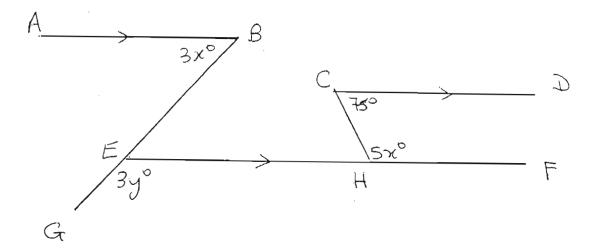


- (i) Find the side length of ABCD. Give your answer in simplified surd form.
- (ii) Find the gradient of the longer diagonal.

1

- (iii) Show that the diagonals of ABCD are perpendicular.
- (iv) Find the coordinates of the midpoint of each diagonal.
- (v) What does this result to part (d) say about the diagonals of this rhombus?
- (vi) Find the equation of the line passing through AC.

Find the value of x and y. Give reasons for each answer.

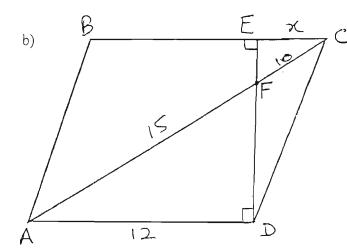


Question 3 (12 marks) (Use a separate sheet of paper)

- a) Differentiate
 - (i) $x^2 e^x$
 - (ii) $\ln\left(\frac{x-5}{x+3}\right)$
- b) (i) Find $\int \frac{dx}{3x-1}$
 - (ii) Evaluate $\int_0^1 e^{4x} dx$, leaving your answer in exact form 2
- c) For what values of m does the equation $4x^2 + (1+m)x + 1 = 0$ have equal roots.
- d) For acute angles A and B it is given that $sinA = \frac{12}{13}$ and $cosB = \frac{15}{17}$ Find the exact value of sec A + tan B.

Question 4 (12 marks) (Use a separate sheet of paper)

a) The sum of the first 4 terms of a geometric progression is 30, and the limiting sum is 32. If the common ratio is negative find the first three terms.



ABCD is a parallelogram.

- (i) Prove that $\triangle EFC$ and $\triangle DFA$ are similar.
- (ii) Find the value of x.

Not to Scale

c) Solve
$$\sin\left(x + \frac{\pi}{3}\right) = 0$$
 for $0 \le x \le \pi$

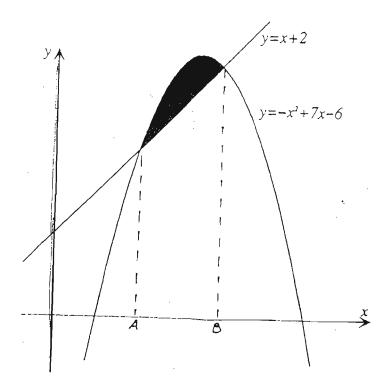
- d) \propto and β are the roots of $2x^2 5x + 5 = 0$. Write down the value of
 - (i) $\propto +\beta$
 - (ii) $\propto \beta$

(iii)
$$\frac{1}{\alpha} + \frac{1}{\beta}$$

Question 5 (12 marks) (Use a separate sheet of paper)

- a) A function is defined by $f(x) = 3x^2 2x^3$
 - (i) Find the coordinates of any turning points and determine their nature 3
 - (ii) Sketch the curve, indicating all intercepts and turning points. 2
 - (iii) State the domain over which both f(x) > 0 and f'(x) > 0
 - (iv) On the same set of axes sketch the line $f(x) = \frac{1}{2}$
 - (v) Hence find the <u>number</u> of solutions to the equation $6x^2 4x^3 = 1$





The diagram shows the graphs of the functions $y = -x^2 + 7x - 6$ and y = x + 2.

- (i) Show that the value of A and B is 2 and 4 respectively
- (ii) Calculate the area of the shaded region.

Question 6 (12 marks) (Use a separate sheet of paper)

a) Evaluate
$$\sum_{r=1}^{4} 3^{r-r}$$

b) For the arithmetic progression 32, 25, 18,

(ii)
$$S_{15}$$

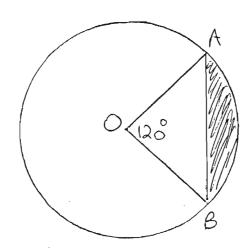
The area under the curve $y = 4^x$ between x = 0 and x = 2 is rotated about the x - axis. Copy and complete the table.

х	0	0.5	1	1.5	2
4 ^{2x}					

Use your results with Simpson's rule to find an approximate value for the volume of revolution. Use 5 function values and answer correct to 1 decimal place.

3

d)



The circle has a radius of 2cm

- (i) Find arc length AB
- (ii) Find the shaded area

. . .

(correct to 1 decimal place)

Question 7 (12 marks) (Use a separate sheet of paper)

a) $f'(x) = 3x^2 - 4$.

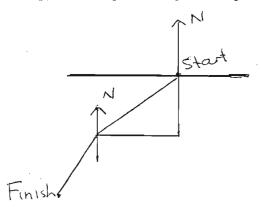
Find y = f(x) if the function passes through (3, 8).

2

b) A boat travels 5km on a bearing of 207° T, then travels 8km on a bearing of 200°T.

Find the straight line distance between the start and finish to 3 significant figures.

Copy and complete the given diagram to assist your working.



\$30 000 is borrowed to buy a car. Interest is charged at 12% pa, compounding monthly. c) The loan is repaid in equal monthly repayments over 4 years. Let A_n be the amount owing after n months. (i) If M is the monthly payment write an expression for the amount owing \propto) 1 month after β) 3 months (ii)Find M Find the total amount paid over the 4 years. (iii) 6 (12 marks) (Use a separate sheet of paper) Question 8 Evaluate lim 2 a) Evaluate $log_5100 - log_54$ 2 b) A particle moves in such a way that its distance, x metres, from the origin c) after t seconds is given by $x = 2 + 3t - t^3$ for t > 0Find an equation for its velocity after t seconds. 1 (i) At what time does the particle stop? (ii)1 Where is the particle initially? (iii) 1 (iv)Find the velocity after 2 seconds. 1 (v)How far has the particle travelled in the first 2 seconds. 2 Find the volume of the solid formed when the curve $y = \sqrt{x}$ is rotated about d) the x axis between x = 1 and x = 5. (leave the answer in terms of π). 2

Question 9 (12 marks) (Use a separate sheet of paper)

a) If
$$F(x) = \begin{bmatrix} x^2 - 2 & x \le -1 \\ 2^x & -1 < x < 2 \\ log_{10}x & x \ge 2 \end{bmatrix}$$

evaluate f(-1) + f(1) + f(10).

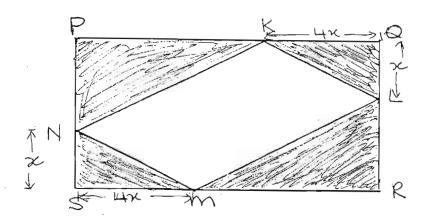
b) Draw a neat sketch of y = 3sin2x within the domain $0 \le x \le 2\pi$.

State the

- (i) period
- (ii) amplitude.

In the diagram, PQRS is a rectangle with PQ=40cm, SP=10cm.

The shaded portions are cut away, leaving the parallelogram KLMN. QL=SN=x cm and QK=SM=4x cm.



(i) Show that the area of the parallelogram KLMN is given by

$$A = 80x - 8x^2$$
.

(ii) Find the allowable values of x

(iii) Find the value of x for which A is a maximum

3

2

4

2

1

Question 10 (12 marks) (Use a separate sheet of paper)

- a) For all values of x in the domain of $0 \le x \le 6$, a function f(x) satisfies f'(x) > 0 and f''(x) > 0.
 - Sketch a possible graph of y = f(x) in this domain.
- b) (i) Find the points of intersection of the curve $y = 4 \sqrt{2x}$ with the x and y axes. 2
 - (ii) The area enclosed by the curve $y = 4 \sqrt{2x}$, the x axis and the y axis is rotated about the y axis. Find the volume of the solid of revolution so formed (leave your answer in terms of π)

4

The line x = m, cuts the curves $y = log_e x$ and $y = log_e 5x$ at R and S respectively.

Show that the tangents to the curves at R and S are parallel. Also show that the distance RS remains constant for all values of M (ie the distance is independent of m).

END OF PAPER

Mathematics 2008
HSC Trial Exam
Question 1 $e^{-0.6} = 0.549 (3ap)$
b) (\overline{12} - 3)^2 = 2 - 6\overline{52} + 9 = 11 - 6\overline{52}
$= \frac{R - P}{PR}$ $\therefore Q = \frac{PR}{R - P}$
$dl(i) \int_{-1}^{2} \frac{dx}{x} = \left[\ln x \right]_{-1}^{2}$ $= \ln 2 - \ln 1$
$\frac{1}{\sqrt{2}} = \ln 2$ $(1i) \int_{\sqrt{3}}^{2} \cos(\frac{x}{2}) dx = 2 \left[\sin(\frac{x}{2}) \right] \eta_{3}$
$= 2\left[\sin\left(\frac{\pi}{4}\right) - \sin\left(\frac{\pi}{4}\right)\right]$ $= 2\left[\frac{\pi}{4} - \frac{1}{4}\right]$ $= 2\left[\frac{\pi}{4} - \frac{1}{4}\right]$
= 52-1
e) $ 2x-3 \le 7$ $ 3x-3 \le 7$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
f) $2x+y=4$ 0 5x+2y=9 (2)

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		× 5	10x + 5	iy = 20.	(3)		
	(2)			iy =20 Hy = 18	Œ	······	
	<u>(</u>	×	10x +	49 = 18):	
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			u =	- 2			
				+2=4			
				2x = 3	<u> </u>		
				x=1			
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Question 2
a) (i) Using A and B
a) (i) Using A and B Side length = $\sqrt{(-5-5)^2 + (q-4)^2}$
$=\sqrt{(10)^2+(5)^2}$
= J125 = 5J5 units
(ii) longer diagonal is AC
(ii) longer diagonal is AC gradient AC = 9-7 -5-7
=-4/2 = M.
(iii) Shorter diagonal is DB
(111) Shorter diagonal is DB gradient DB = -2-4 -3-5
= -6
$=3/4=m_{2}$
$N_0\omega = \frac{3}{4} = m_2$ $N_0\omega = \frac{-4}{3} \times \frac{3}{4}$
= -
Sortisfies condition for perpendicular line diagonals perpendicular
diagonali perpendicular
(IV)
$M = \begin{pmatrix} -5+7 & 9+-7 \\ \hline & & 2 \end{pmatrix} \qquad M = \begin{pmatrix} -3+5 & -2 \\ \hline & 2 \end{pmatrix}$
= (1, 1) = (1, 1)
= (1,1) = (1,1) (v) Result confirms diagonals bisect, at (1,1)
(vi) Gradient AC = -4/3
(vi) Gradient AC = $-\frac{4}{3}$ Eqn AC : $y-q=-\frac{1}{3}(x+45)$
3y - 27 = -4x - 20.
4x + 3y - 7 = 0

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	3x°/	(7750			*********
F/			/42			
/3y°			Н		F	
4			-7			
Since	CD HH	<u> </u>	75° +	5 x =	180°	
<u>1e'</u> 0	ointerior 5	angles	supple	menta	ry	
	. 5	X = 10	5	***************************************		
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	1	7		an	der egue	<u>. () </u>
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					1800)	
But >	k= 21					
	3 <u>U</u>					
		y = 3	} a			
		9				
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uestion 3		- \ - \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	(d)	
vestion 3 (i) $y = x^2 e^x + 2x(e^x)$	U= X	$\frac{1}{N} = \kappa$		\
$y' = x^2 e^x + 2x(e^x)$	n =3x	<u>√</u> = €		13 ·
$= \chi e^{\chi}(\chi + a)$		-	12	
				, 5 \A
$(11) y = \ln\left(\frac{x-5}{x+3}\right)$				
$= \ln(x-5) - \ln(x+3)$			Convole	te each trian
$y' = \frac{1}{x-5} - \frac{1}{x+3}$,	
				secA + to
= x(+3-(x-5)				
(x-5)(x+3)				
= 8 (x-5)(x+3.)		and the state of t		
(x-5)(x t 3.)				
dy				
(3x-1)	+ C			
9				**************************************
(ii) $\int_0^1 e^{+x} dx = \left[\frac{1}{4} e^{+x}\right]_0^0$				
= +e - +				
= 46 - 4	2			
	1/_4	7		
= 12 - 1	= 4/6-	1)		
c) $4x^2 + (1+m)x + 1 = 0$,,			
Equal roots when 0=	<u> </u>		į	
$\Delta = b^2 - 4ac$				
= (1+m)²-4(4)(1)				
= 1 + 2m +m = 16				
= m + am -15				
Solve m + 2m - 15 = 0	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		11.0	
(m.4.5)(m3)				
m=-5 of M=	3			

d) N	
13 .	17.
12	8
h 5 \A	h B
	15
_ 1 :	
Complete each trian	sale
,	
secA + to	mB=== + 15
	= 39 +8
	= <u>39 + 8</u> IS
	= 47
	15:
,	

Question4
$S_n = \frac{\alpha(1-1)^n}{n}$
8 - 0(1, 4)
$3\mu = \alpha(1-r^{4}) = 30$
So = - 32
$1' \cdot \ln SH + 32(1-r^{4}) = 30$ $1-r^{4} = \frac{30}{32}$
14 = 30
$r^{4} = \frac{2}{37}$ $= \frac{1}{16}$
$\Gamma' = \overline{3}$
$V = \pm \frac{1}{2}$
$r = \pm \frac{1}{2}$ But $r < 0$ if $r = -\frac{1}{2}$ and $a = 48$
1 7 . 110
T ₁ = 48
$T_2 = -a4$
$T_3 = 12$
b) B E x C
ExC [] [FEC = [FDA = 90 (given)] [EFC = [AFD (vertically)] opposite angles equal)
(1) I = 10 (given
15 (Vertically
opposite angler equal)
1 V
A 12 D : DEFC and DPA are
equiangulas
: Jimilar
(ii) Corresponding sides are in the same ratio
,
$\begin{array}{cccc} & \times & = & \times & \times \\ & \times & \times & \times & \times & \times \\ & \times & \times & \times & \times & \times \\ & \times & \times & \times & \times \\ & \times & \times & \times & \times \\ &$
24
X = 3
= 8

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For given domain: $\chi = 2\pi/3$	27, 37, 27 ₃ , 57 ₃ , 87 ₃ ,
d) $2x^2 - 5x + 5 = 0$ (1) $2x + \beta = \frac{5}{2}$ (ii) $2x + \beta = \frac{5}{2}$ (iii) $2x + \beta = \frac{5}{2}$ $2x + \beta = 0$ $2x + \beta = 0$	2
= 1	
,	
· · · · · · · · · · · · · · · · · · ·	

 $f(\alpha) = 3\pi c^2 - 2\pi^3$ Question 5 for turning points (stationary) P'(x)=0 : Solve 6x(1-x)=0 X=0 , X=1 f'''(x) = 6 - 12x f'''(x) = 6 - 12x f'''(x) = 6 - 12x f'''(x) = 6 - 12x(i) = 6-12 20 => max " min at (0,0) max at (1,1) (ii) f(x) = 0 when $\chi^2(3-2x) = 0$. Let $\chi = 0$ or $\chi = \frac{3}{2}$ (iii) f(x) >0 above y axis } Both hold for f(x) >0 increasing] 0 < x < 1 (iv) $f(x) = \frac{1}{2}$ (above) (v) $6x^2 - 4x^3 = 1 = 3x^2 - 3x^2 = \frac{1}{2}$ Since $f(x) = 3x^2 - 2x^3$ and $f(x) = \frac{1}{2}$ Intersect 3 times, there will be 3 solutions

k	$y = -x^2 + 7x - 6$ $y = x + 2$
	(i) Intersect when
ļ	$-x^2 + \frac{1}{2}x - 6 = x + 2$
	<u>le' x2 -6x +8 =0</u>
ļ	$(\chi - \mu)(\chi - 1) = 0.$
	X= 2 or X=4
	From graph A= 2
	8=4 \ (\frac{1}{2} - 1) \ (\frac{1}{2} - 1)
(ii) Area = $\int_{2}^{4} \left(-x^{2} + 7x - 6\right) - (x + a) dx$
	= (" (-v² +1, -8) dy
	$= \int_{2}^{4} \left(-x^{2} + 6x - 8\right) dx$
	$= \left[-\frac{1}{3}x^3 + 3x^2 - 8x \right]$
	-
	$= -\frac{1}{3}(64) + 3(16) - 32 - (-\frac{8}{3} + 12 - 16)$ $= -\frac{1}{3} + 48 - 32 + \frac{8}{3} - 12 + 16$
	= -64 + 48 - 32 + 8/3 - 12 + 16
	= -56 + 20 = $1/3 u^2$
	$=\sqrt{2}$ u.
\	
1	
,	
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Destion b	!
a) $5 3^{1} = 3 + 3 + 3^{-2} + 3^{-3}$	
= (13/27	
b) 3a, as, 18 ··· a=32, d=-7	
$(1) T_{15} = a + 14d$	
$= 32 + 14 \times (-7)$	
= 32 - 98	
= - 66	}
$(1i) S_{15} = \frac{15}{2} \left[3a + 14d \right]$	
= \[\begin{align*} \b	
= 15[32 - 49]	
$=15\times-17$	
= -255	
(iii) Sum next 20 terms	
= 537-515	
3)	
$=\frac{35}{2}[64 + 34 \times (7)] - (-255)$	***
=35[32 + 17 × (-7)] + 255	
3045 +255	
= -2790	****
<u>C</u>)	
x 0 0.5 1 1.5 2	
4 ^{2x} 1 4 16 64 256	
yo y, 72 43 44	*****
Vol = Tr (4 dx	
6	-
= T 3 (yo ty, + 4×(4, +y3) +2(y2)) \
0 11 5 13 13 13 13 13 13 13 13 13 13 13 13 13	
= 1 [6 (1+256 + 4 (1-8) + 2 (16)]	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
=11 [[1 + 970 + 41(2) + 2(10)]	,
the grant of the control of the cont	

Vol = π[t (5b1)]	
$= 293.7 u^3 (1dp)$	
$A) (1) 50_0 = \frac{3}{50}$	
$= 2 \binom{211}{3}$ $= 411 \text{ cm}$	
(ii) Area = $\frac{1}{2} r^2 (o^c - sino^c)$ = $\frac{1}{2} (4) \left[\frac{24}{3} - \frac{13}{2} \right]$	
$= 2\left(\frac{3\pi}{3} - \frac{\sqrt{3}}{3}\right) \epsilon m^2$	
- 2(3 =) cm	

Question ?
a) $f'(x) = 3x^2 - 4$
$f(x) = \chi^3 - 4 \times 4 C$
(38) satisfies
$1.8 = 3^3 - 4(3) + C$
8 = 27-24 C=> C=-7
$1.4 = x^3 - 4x - 7$
b) Angle at A= 63+90 +20
d= distance s-7F
o A 63/ Fl i. By corne rule
$\frac{1}{2} = 5^{2} + 8^{2} - 2 \times 5 \times 8 \cos 173^{\circ}$ $= 25 + 64 - 80 \cos 173^{\circ}$
= 89 - 80 cos 173°
Finish d2 = 168.4036921
11.d=12.97704482 =13.0 km(3 sig figs)
213.0 km 2319 1.03
1 1 201 - 101- Dar month
c) \$30000 12° 0 pa= 1° 10 per month 48 repayments
(1) 2) A = 30000 (1.01) - M
(1) 2) A, = 50000 (1. st.)
m = (10.1) - m = (1.01) - m
β) $A_2 = \frac{30000(1.01) - m}{30000(1.01)^2 - m(1.01 + 1)}$
Similarly 3 all ni 11 or th
$N = 2 - 200 \left(\frac{1}{100} \right) - \frac{1}{100} \left(\frac{1}{100} \right) = \frac{1}{100} \left(\frac{1}{100} \right) $
(ii) Aus = 0 since fully repaid
(11) 1748 - 9 31.10
0 = A48 = 3000 (1.01) -m (1.01 + 1.01 +
The state of the s
$\frac{12}{12} 30000 (1.01) = m(1 + 1.01 + + 1.01)$ $\frac{12}{12} 30000 (1.01) = m(1 + 1.01 + + 1.01)$
N=48
,一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就是一个人,我们就
The state of the s

	$M = 30000(1.01)^{48}$
	1-1.01
	= 30000(1.01)48 (0.01)
	1.0149-1
	= \$790.00 (nearest cont)
(iii)	Total repaid = M × H8 = \$37920.72 (newest cen
	= \$37920.72 (nowest cen
······	

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Question 8 Sin2x lim (sin2x) x 2
Question 8 a) $\lim_{x\to 0} \frac{\sin 2x}{x} = \lim_{x\to 0} \left(\frac{\sin 2x}{2x}\right)_{x} = \frac{\sin 2x}{2x}$
b) $\log_{5} 100 - \log_{5} 4 = \log_{5} (\frac{100}{4})$
$= \log_5 35$ $= \log_5 5^{\frac{1}{2}}$
= logs 5
c) $x = 2 + 3t - t^3$, $t > 0$
c) $x = 3 + 3t - t^3$, $t > 0$ (i) $dx = 3 - 3t^2$ dx
$vel = 3 - 3t^{2}$
(ii) Story when V=D
(ii) Stops when $V=0$ Le Solve $3-3t^2=0$ t=1 ($t>0$)
SL or ofter 1 Second
Stops after 1 second (iii) $t=0$ in $x=a+3t-t^3$
: Initially 2m to the right of O.
(IV) When t=2
(iv) When $t=2$ $v=3-3(a)^2$
$\frac{1}{12} v = -9 \text{m/sec} \text{(travelling to the left)}$
(V) (2) t=0.
0 2 4
When $t=1$, $x=2+3-1$
t=2, x=2+6-8
= 0
The state of the s

	Has trav	elled 2 + 14 = 6 m
d).	J-Var	$V_0 = \pi \int_1^{\infty} x dx$
		$=\pi\left[\frac{3}{2}x^{2}\right]$
		$\frac{3}{11} \left[32 - 1 \right]$
		= 12 T U
		!
	en e	

Question 9 :. f(-1)+f(1)+f(10)=2 b) y=3 sin 2x (i) Period = 2 (ii) Amplitude = 3 K 4x & locm S 4x m 40 cm (i) Area parallelo gram HMN $= 40 \times 10 - 3 \times \frac{1}{2} (4x)(x)$ $- 3 \times \frac{1}{2} (40 - 4x)(10 - x)$ =400-4x2-(400-40x-40x = 80x - 8x2

(ii) 0 < x < 10	
$\frac{(lii)}{dx} = 80 - 16x$	
$\frac{dR}{dx} = 0 \text{when} 16x = 80$ $x' = 5$	
$d^2\Lambda = -16 \langle 0 \rangle = 2 \text{ max}$	
Area max when x=5:	
	·

Duestion 10	6 fix)>	o P" (x) >	· Q
19	increas	sing conco	me up.
) x		
		-	
b) (1) y=1 x axi	y=0 <u>re</u>	$\sqrt{3x} = 4$	
	V	x = 8.	
y ax	s: x=0	é y=4	
(ii) \(\frac{\frac}\firk}{\firac{\frac{\frac}}}}}{\firac{\frac{\frac{\frac{\frac}}}}{\firac{\frac{\fir}{\fired{\frac{\fir}}}}}{\frac{\frac{\fir}{\firac{\fir}{\fired{\frac{\fir}}}}}{\frac{\frac{\frac{\frac{\fir}{\fir}}}}}}}{\frac{\frac{\frac{\fir}{\firac{\fir}{\firac{\fir}}}}{\frac{\frac{\frac{\frac{\frac}{\frac{\frac{\frac{\frac{\fir}}}}}}{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{		y = 4 - Jax Jax = 4-y	
4		2x = (4-4)	
2	4 6 8	$\chi = H^{-2}$	
	$\langle 0 = T \int_{0}^{1} x^{2} dx$	М	
	=17 (4-1	<u>3) </u>	
	= 17 [(4-)	3) [] (
	= -20 [(M-12/8 - (H-0)	
	= -50	- 4)5 - 4) - 201	T 3
pour comment of a survey of state of a survey of state of the survey of state of state of the survey of state of stat	20 X	154 = 256	V.

***************************************	C) $y = \log_e x$ $y = \log_e 5 + \log_e x$
Up.	. /. 5
	100ge 2 R
	x=m,
	$y = \log_e x$ $y = \log_e x$ $y' = 0 + \frac{1}{2}$
,	$A \vdash R, x = m$
	grad = to At S, x=m
****	: grad = in
	They have the same gradient. Tangents are parallel.
	$P = (m, log_e m)$ $S = (m, log_e 5 + log_e m)$
	RS = \((m = m)^2 + (loge m - (loge s + loge m))^2
	= V(log_5)
	= log_5 : ls remains constant
	Je
	CNE
3	